

# ECDSA gem

[https://github.com/DavidEGrayson/ruby\\_ecdsa](https://github.com/DavidEGrayson/ruby_ecdsa)

David Grayson  
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# ECDSA

- Elliptic Curve Digital Signature Algorithm

# Elliptic Curve Space

- 2-dimensional
- A point has two coordinates,  $x$  and  $y$
- $x$  and  $y$  are integers between 0 and  $p-1$ , where  $p$  is a pre-defined large prime

# Elliptic Curve

- Curve equation, modulo prime  $p$ :

$$y^2 = x^3 + ax + b$$

# Elliptic Curve Group

- Need to define addition of points
- Need to pick a generator point  $G$
- The curve group is made up of these points:

$$\infty, G, G+G, G+G+G, \dots$$

- The words “group” and “curve” are often used interchangeably in ECDSA.

# These parameters define an Elliptic curve:

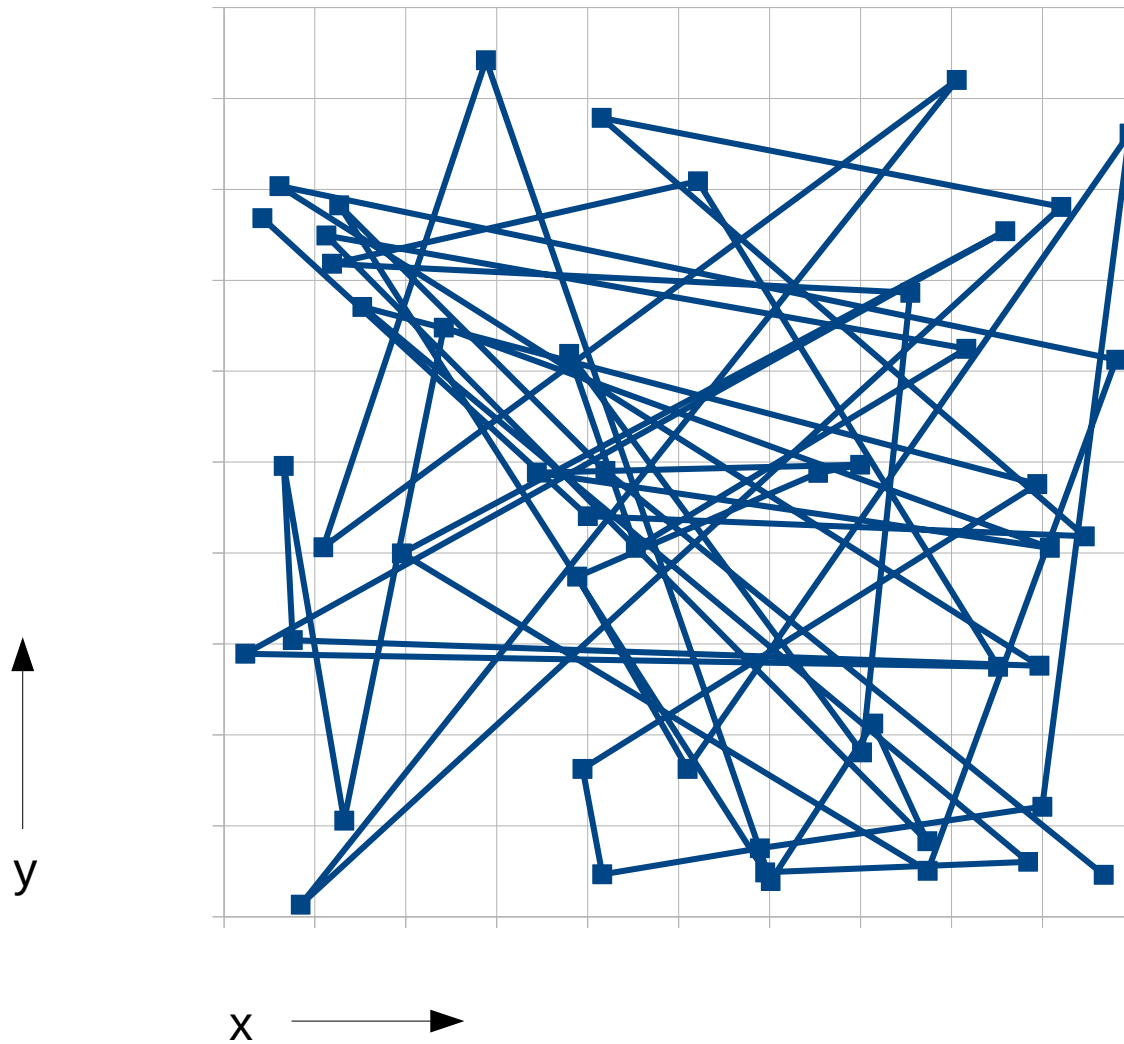
- $p$ : prime that defines the range of the coords
- $a$ : coefficient in the curve equation
- $b$ : coefficient in the curve equation
- $G$ : the generator point

# Example curve parameters

```
module ECDSA
  class Group
    Secp112r1 = new(
      name: 'secp112r1',
      p: 0xDB7C_2ABF62E3_5E668076_BEAD208B,
      a: 0xDB7C_2ABF62E3_5E668076_BEAD2088,
      b: 0x659E_F8BA0439_16EEDE89_11702B22,
      g: [0x0948_7239995A_5EE76B55_F9C2F098,
          0xA89C_E5AF8724_C0A23E0E_0FF77500],
      n: 0xDB7C_2ABF62E3_5E7628DF_AC6561C5,
      h: 1,
    )
  end
end
```



# secp112r1 curve visualization



# Private key

- A private key is just an integer  $d$

```
require 'ecdsa'  
require 'securerandom'  
group = ECDSA::Group::Secp256k1  
private_key = 1 + SecureRandom.random_number(group.order - 1)  
puts 'private key: %#x' % private_key
```

- The public key is  $G$  added to itself  $d$  times.

```
public_key = group.generator.multiply_by_scalar(private_key)  
puts 'public key: '  
puts '  x: %#x' % public_key.x  
puts '  y: %#x' % public_key.y
```

# Signing and verifying

```
require 'digest/sha2'
message = 'ECDSA is cool.'
digest = Digest::SHA2.digest(message)
signature = nil
while signature.nil?
  temp_key = 1 + SecureRandom.random_number(group.order - 1)
  signature = ECDSA.sign(group, private_key, digest, temp_key)
end
puts 'signature: '
puts '  r: %#x' % signature.r
puts '  s: %#x' % signature.s
```

```
ECDSA.valid_signature?(public_key, digest, signature)
```

# ECDSA gem design decisions

- Value education/experimentation over efficiency
  - Cryptographic code, not cryptic
  - Avoid OpenSSL as much as possible
- No randomness
  - Let the user choose a random number generator
- Separation of concerns between cryptography and binary data formatting
  - Cryptographic classes work with Ruby integers

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